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## Validation of a generalized laser safety analysis method for irregular pulse trains

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#### ABSTRACT

The current laser safety standards do not address specifically how to account for repetitively pulsed lasers with irregular pulse trains. Variations in peak power, pulse duration, and duty cycle within a pulse train pose a number of problems when it comes to product classification or to assess the hazard of a given exposure. This study proposes to analyze irregular pulse trains by generalizing the determination of the number of pulses N used in the IEC 60825-1 or n in the ANSI Z136.1 standard. The proposed method for the determination of N applies to emission durations longer than 5 µs and was validated by generating a large number of theoretical pulse patterns and by comparing the retinal injury threshold, determined with a computer model, with the applicable emission limit. For 18 000 different pulse patterns, the ratio of the injury threshold to the emission limit was never less than 2, which is commonly considered as a sufficient safety margin. The smallest safety margin found for regular pulse patterns also equals 2. This study validates an analysis method for irregular pulse trains that can be included in the standards by simple generalization of the determination of the parameter N.

Key words: laser safety, retinal damage, computer model, pulse train, classification, IEC 60825-1, ANSI Z136.1

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# Validation of a generalized laser safety analysis method for irregular pulse trains

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#### **ABSTRACT**

The current laser safety standards do not address specifically how to account for repetitively pulsed lasers with irregular pulse trains. Variations in peak power, pulse duration and duty cycle within a pulse train pose a number of problems when it comes to product classification or to assess the hazard of a given exposure. This study proposes to analyze irregular pulse trains by generalizing the determination of the number of pulses *N* used in the IEC 60825-1, or *n* in the ANSI Z136.1 standard. The proposed method for the determination of *N* applies to emission durations longer than 5 µs and was validated by generating a large number of theoretical pulse patterns and by comparing the retinal injury threshold, determined with a computer model, with the applicable emission limit. For 18,000 different pulse patterns, the ratio of injury threshold to emission limit was never less than 2, which is commonly considered as a sufficient safety margin. The smallest safety margin found for regular pulse patterns also equals 2. This study validates an analysis method for irregular pulse trains that can be included in the standards by simple generalization of the determination of the parameter *N*.

#### **Keywords**

Laser safety, retinal damage, computer model, pulse train, classification, IEC 60825-1, ANSI Z136.1.

#### I. INTRODUCTION

For irregular pulse trains, one or more of the following parameters varies: the energy per pulse, the pulse duration or the pulse interval. Irregular pulse trains are common to many types of laser products. For instance for scanned emission, such as found in many lidars and 3D cameras, that scans both horizontally as well as vertically, even a continuous (non-pulsed) emission results in an irregular ocular exposure as a consequence of the stationary circular aperture representing the pupil of the eye. Products with stationary beams can also feature emission with varying pulse durations or peak power, for instance range finders optimized to operate at different distance ranges. The proposed method is not relevant for the case of regular pulse patterns that are, for example, possible for ophthalmic instruments with scanned beams where the beam is not clipped by the pupil of the eye (e.g. maxwellian view).

In 2014, the third edition of IEC 60825-1 [1] as well as a new edition of ANSI Z136.1 [2] were published. In both standards, the rules of how to apply maximum permissible exposure values (MPE) or accessible emission limits (AEL) to repetitively pulsed lasers are identical for pulse or emission durations longer than the parameter  $T_i$  or  $t_{min}$ , symbol used in IEC 60825-1 and ANSI Z136.1, respectively. This parameter is equal to 5 µs in the wavelength range of 400 nm to 1050 nm and equal to 13 µs between 1050 nm and 1400 nm (see subclause 4.3 f) in IEC 60825-1:2014; 8.2.3 and Table 6c in ANSI Z136.1-2014). The two standards differ only for pulse durations shorter than  $T_i$  (or  $t_{min}$ ), where the correction

factor  $C_5$  is applied in the IEC 60825-1, while there is no such correction in the ANSI Z136.1 standard. In the following, we will only refer to the IEC 60825-1 standard but the discussion applies to both standards. The pulse duration domain less than 5  $\mu$ s is, however, not in the scope of the present work.

The changes of IEC 60825-1:2014 in comparison to earlier editions were reviewed in a white paper [3]. Specific issues related to the analysis of repetitively pulsed emissions were addressed in a proceeding paper [4] and published in an Interpretation Sheet (ISH1) for IEC 60825-1 in 2017 [5]. The analysis of a repetitively pulsed emission relies on the application of three rules (or criteria), often referred to as single pulse, average power and reduced pulse criterion. These criteria are concomitant in order to cover different biophysical aspects and the most restrictive result is defined as the highest ratio of accessible emission (AE) to AEL. In IEC 60825-1, the term accessible emission, AE, is used to refer to the quantity that is compared against the AEL, and when the AE is smaller than the respective AEL (such as for Class 1) for all conditions required in the standard, the product is assigned the respective class, such as Class 1. The specific term AE is used to highlight that there is a range of rules to consider for the determination of the AE, such as with specific aperture stop diameters and angle of acceptances. The main interest of this paper is the classification of a laser product as Class 1 for wavelengths between 400 nm and 1400 nm where the retinal thermal AEL applies, as shown in Eq. (1) for the visible wavelength range and emission durations t between 5  $\mu$ s and  $T_2$ .

$$AEL[J] = 7 \cdot 10^{-4} C_6 t^{0.75} \tag{1}$$

Where

$$T_{2}[s] = \begin{cases} 10 & \text{if } \alpha \leq \alpha_{min} \\ 100 & \text{if } \alpha > 100 \text{ mrad} \\ 10 \cdot 10^{(\alpha - \alpha_{min})/98.5} & \text{otherwise} \end{cases}$$
 (2)

Therefore, when we refer to AEL, the retinal thermal AEL for Class 1 is meant, unless otherwise noted. The analysis in principle is equivalent for classification of laser products as Class 2, where the maximum emission duration to be considered is limited to the time base of 0.25 s. In this paper, for the application of the method to Class 2, the time base of 0.25 s has to be used whenever we refer to  $T_2$  (the emission duration from which onwards the AEL is a constant power value). The parameter  $T_2$  is a function of the angular subtense of the image of the apparent source  $\alpha$  as shown in Eq. (2) where  $\alpha_{min} = 1.5$  mrad.

The following gives a brief overview of the three pulse evaluation criteria that apply to classification as Class 1 in the retinal thermal regime:

#### 1) Single pulse criterion

The accessible emission of a pulse has to be below the AEL(t) for the duration t of that pulse, AEL<sub>single</sub>(t). In the case of an irregular pulse train (in the following, the abbreviation IPT is used), each and every pulse must be compared against the applicable AEL(t).

#### 2) Average power criterion

The accessible emission AE(t), determined as average power, averaged over a duration t, is compared against the AEL(t) applicable for that duration t. In IEC 60825-1, the symbol  $AEL_T$  is used, where T is the averaging duration. For regular pulse patterns, i.e. a pattern that fulfills three conditions, namely constant pulse duration, constant energy per pulse and constant pulse interval (i.e. constant pulse frequency), the most restrictive averaging duration is always  $T_2$ . In the case of an IPT, the averaging duration t must be varied between  $T_i$  and  $T_2$  in order to verify that the AE(t) is below the AEL(t) for all averaging durations and temporal positions of the averaging time-window within  $T_2$ . In the case of an emission where the temporal irregularity extends over periods that are longer than  $T_2$ , it is also necessary to shift the averaging time-window of  $T_2$  so as to find the most restrictive ratio of AE(t) to AEL(t). We note that to compare the average power (averaged over a certain duration t) against the AEL(t) expressed as power is equivalent to compare the energy within that time t against the AEL(t) expressed as energy, i.e. the ratio of AE(t)/AEL(t) does not change.

#### 3) Reduced pulse criterion

The accessible emission of a pulse, or that of a group of pulses, has to be below the AEL<sub>s.p.train</sub>(t) for the duration t of that pulse or pulse group. AEL<sub>s.p.train</sub>(t) can be understood as reduced single pulse AEL and is the product of AEL<sub>single</sub>(t) and a correction factor  $C_5$  (referred to as  $C_P$  in ANSI Z136.1).  $C_5$  varies between 0.2 and 1, depending on the parameter N (referred to as the 'effective number of pulses') determined for the time period  $T_2$ . The specific formula to use for  $C_5$  also depends on the applicable emission duration t (i.e. the duration of a pulse or of a group of pulses) and the angular subtense of the image of the apparent source  $\alpha$  as illustrated in Eq. (3) for  $t > T_i$  (see additional details in Clause 4.3 f) of IEC 60825-1:2014 as well as discussion by Schulmeister [4]).

$$C_5 = \begin{cases} 1 & \text{if } \alpha \leq 5 \text{ mrad or } \alpha > 100 \text{ mrad} \\ \max(0.4, N^{-0.25}) & \text{if } 5 \text{ mrad} < \alpha \leq \alpha_{max} \\ \max(0.2, N^{-0.25}) & \text{if } \alpha > \alpha_{max} \end{cases}$$
(3)

For regular pulse patterns, the application of the reduced pulse criterion is based on the number of pulses within  $T_2$  and the energy per pulse, where it is not necessary to consider groups of pulses as if they were pulses. For an IPT, additionally to considering single pulses for criterion 3), groups of pulses have to be analyzed, i.e. each group is treated as an 'effective pulse' (see also ISH1 [5]). For such an analysis of groups of pulses, the duration of the group is used to determine  $AEL_{single}(t)$ . The accessible emission is the energy within that group and N is the number of groups within  $T_2$ . As a general method, the emission duration t for which the accessible emission and AEL(t) are determined can be seen as a time window over which the energy is summed up. There is no specific term and symbol used in the current edition of IEC 60825-1, and we will refer here to the evaluation duration  $\Delta t$ . Thus, the AE is the energy summed up within  $\Delta t$  and the sum has to be below AEL<sub>s.p.train</sub>( $\Delta t$ ). Since the limiting angular subtense  $\alpha_{\max}(\Delta t)$  is also determined with  $\Delta t$ , the value of  $\alpha$  in  $C_6$  ( $C_6 = \alpha / \alpha_{min}$ ) as well as the angle of acceptance for the determination of the AE can vary depending on the value of  $\Delta t$  (see for instance Schulmeister 2015 [6] for a detailed discussion on these parameters of the standard). In the general scheme, the evaluation duration  $\Delta t$  is varied both in terms of the temporal start position within the pulse train and in terms of the duration (between  $T_i$  and 0.25 s; emission durations longer than 0.25 s are not considered as pulses and  $C_5$  is not applied). Without specific rules how to determine N for an IPT, each pulse or pulse group has to be counted, irrespective of how small the peak power or energy is compared to the other pulses (or pulse groups) in the pulse train.

Thus, when each pulse is counted as 1, the parameter N does not reflect the fact that pulses with relatively low peak power are inherently less hazardous as a consequence of the lower energy deposition rate. Some effort has been done in the past years for the laser safety standards to better address the issue of irregular pulsed emissions. In the specific case of constant pulse duration and varying peak power [7], specific guidance has been published in an IEC document [5] as a complement to IEC 60825-1 Edition 3.0. It specifies that N can be determined based on the fraction of the relative peak powers of the pulses. This is, however, not applicable in the general case where both peak power and pulse duration vary.

The present study intends to demonstrate that irregular pulse trains can be properly evaluated when the parameter N is determined as the ratio of the energy within  $T_2$  to the energy within the evaluation duration  $\Delta t$  (see detailed discussion of the method in the next section). The intention behind this proposal is to provide a solution that does not require any modification of the existing classification rules and is applicable to any pulse train with pulses in the thermal damage mechanism regime, i.e. for pulse durations longer than  $T_i$ . Since the computer model employed for validation is not applicable for the regime where the damage mechanism is micro-cavitation [8], at this point in time it is unfortunately not possible to assess if the proposed method is also valid for the case that the emission contains pulses with duration shorter than  $T_i$ .

#### II. MATERIALS AND METHODS

#### A. Analysis method to be validated

The parameter N used to calculate the correction factor  $C_5$  in IEC 60825-1 (or n and  $C_P$  in ANSI Z136.1) is referred to as the 'effective number of pulses' (this term implies that N is not necessarily the actual number of pulses within the specified evaluation period). In the following we refer to  $T_2$  as the period to determine N, which is applicable for classification as Class 1 laser product. For the case that the time base equals 0.25 s, i.e. for Class 2 classification,  $T_2$  has to be replaced accordingly. It is proposed, for future editions of IEC 60825-1, to determine N (see Eq. (4)) by the ratio of energy  $Q_{T_2}$  within the emission duration  $T_2$  to the energy  $Q_{\Delta t}$  within the evaluation duration  $\Delta t$  (representing a pulse or a group of pulses within  $T_2$ ).

$$N = \frac{Q_{T_2}}{Q_{\Lambda t}} \tag{4}$$

As is already the general requirement to analyze groups of pulses as 'effective pulses' (see Interpretation Sheet 1 [5]), both the duration of  $\Delta t$  and the temporal position within  $T_2$  (the start time of  $\Delta t$ ) must be varied to cover individual pulses but also groups of pulses up to a duration of 0.25 s (the maximum duration to be considered for a pulse or group of pulses). Thus, for irregular pulse trains, this method of considering the energy within a certain evaluation period to encompass single pulses but also groups of pulses (here given the symbol  $\Delta t$  and to be varied in temporal start position and duration) is already necessary, based on IEC 60825-1:2014 and the associated Interpretation Sheet ISH1 [5]. The difference to the existing required method is that N is not equal to the number of pulses or pulse groups, but is determined in a more general way. Thus we emphasize that for this method, for irregular pulse trains, N is not the number of pulses or the number of pulse groups within  $T_2$ , and we therefore in the following also avoid using that terminology and refer to the parameter N only - as the parameter relevant for the determination of  $C_5$ . It is also apparent that the numerical value of N determined with the proposed method, for irregular pulse trains, is different to when N is the number of pulses or the number of pulse groups within  $T_2$ . In order to facilitate the use of symbols and the flow of reading, the symbol N is used and not a different symbol. It is pointed out, however, that for pulse trains with constant energy per pulse Q (or groups of pulses with constant energy per group), the value of N determined by the proposed method is equal to the number of pulses (or pulse groups, respectively), because the total energy within  $T_2$  is  $Q_{T2} = N \cdot Q$ .

For a simple pulse pattern, the choice of the evaluation durations can be based on the pattern at hand, but it can also be automated by a computer program to analyze the pulse train data. We note that the variation of the evaluation duration  $\Delta t$  in terms of start time and duration is equivalent to the requirement for the average power criterion to vary the averaging duration. The evaluation duration  $\Delta t$  is used to calculate the accessible emission limit  $\text{AEL}_{\text{single}}(\Delta t)$  as well as  $\alpha_{\text{max}}(\Delta t)$ , which is relevant for the determination of  $C_6$  and of the accessible emission. The value of N that is determined for a specific duration and position of  $\Delta t$  is used to calculate  $C_5$  and  $\text{AEL}_{\text{s.p.train}}(\Delta t)$  for that evaluation duration. The energy  $Q_{\Delta t}$  can be seen as the accessible emission AE that applies to the evaluation duration that is analyzed, although for the determination of N as a ratio a relative value can be used instead of the absolute value of  $\text{AE}(\Delta t)$ . As is the general classification principle, the AE has to be below  $\text{AEL}_{\text{s.p.train}}$  for all durations and positions of  $\Delta t$  within  $T_2$ . This can also be understood as the process to determine the evaluation duration  $\Delta t$  which features the maximum ratio of AE/AEL and this particular evaluation duration is then used for classification according to the reduced pulse criterion.

We note that for the determination of N based on our proposal, the field-of-view (i.e. the angle of acceptance) must be identical for both components of the fraction. In other words, both  $Q_{T_2}$  and  $Q_{\Delta t}$  must be determined for the same angle of acceptance. For a stationary retinal image, the choice of the field-

of-view does not affect the energy ratio, i.e. it is possible to use a field of view that is larger than the image of the apparent source, also referred to as an open field of view.

In the case of pulses defined by a rectangular temporal function, the above formula can be rewritten as

$$N = \frac{\sum_{k=1}^{K} P_k \cdot t_k}{\sum_{m=1}^{M} P_m \cdot t_m} \tag{5}$$

where K is the number of pulses within  $T_2$  and M is the number of pulses within the evaluation duration,  $\Delta t$ . Thus, M pulses within  $\Delta t$  are a subset of the K pulses within  $T_2$ .  $P_k$  and  $P_m$  are the respective peak powers,  $t_k$  and  $t_m$  are the respective pulse durations of the rectangular temporal functions. For this method to determine N, it is proposed to neglect all pulses with a relative peak power below 5 % of the highest peak power when determining  $Q_{T_2}$  and  $Q_{\Delta t}$  and when selecting the interval  $\Delta t$ , i.e. these pulses are purely removed from the AEL analysis. All existing classification rules, criteria and parameters given in IEC 60825-1:2014 are applicable. The method can also be applied for an MPE analysis as described in Annex A of IEC 60825-1 or for an analysis based on ANSI Z136.1.

The arbitrary pulse pattern shown in Fig. 1 is used to illustrate the calculation steps for deriving AEL<sub>s,p,train</sub>( $\Delta t$ ). The angular subtense of the image of the apparent source is assumed to be equal to 10 mrad and the profile is circular and homogeneous, i.e. top-hat. The evaluation duration  $\Delta t$  is varied to apply to each pulse, as well as to groups of pulses. It is assumed that besides the four pulses shown in Fig. 1, there are no other pulses within  $T_2$ . For each choice of evaluation duration  $\Delta t$  (and start position), the AEL<sub>single</sub>( $\Delta t$ ) is determined for that duration  $\Delta t$ , also considering the limitation of  $\alpha_{\max}(\Delta t)$  and in turn  $C_6$  that depends on the choice of the duration of  $\Delta t$ . For instance, for the first pulse with a pulse duration of 1 ms,  $\alpha_{\text{max}}(\Delta t) = 6.3$  mrad. For each chosen evaluation duration, AEL<sub>single</sub>( $\Delta t$ ) is reduced by  $C_5$  to obtain AEL<sub>s,p,train</sub>( $\Delta t$ ), where  $C_5$  is determined as the ratio of the energy in the total pulse pattern  $Q_{T_2}$ (taken here as 50  $\mu$ J) to the energy within the evaluation duration  $Q_{\Delta I}$ . For the first, second or fourth pulse,  $Q_{\Delta t}$  equals 10  $\mu$ J and therefore N is in those cases 50  $\mu$ J / 10  $\mu$ J = 5. For the third pulse,  $N = 50 \,\mu\text{J} / 20 \,\mu\text{J} = 2.5$ . To determine N, the values of  $Q_{\text{T}_2}$  and  $Q_{\Delta t}$  are assessed here in terms of the total intraocular energy, i.e. with an open field view. The same ratio would result when, for instance, an angle of acceptance equal to  $\alpha_{\max}(\Delta t)$ , or any other angle of acceptance, were applied. We note that in this example, for applying  $\Delta t$  to the first, second or fourth pulse, it results a value of N larger than the actual number of pulses in the pulse pattern. Also groups of pulses need to be analyzed, such as the first and second pulses as a group, resulting in  $N = 50 \,\mu\text{J} / 20 \,\mu\text{J} = 2.5$ . The AE for the respective evaluation duration  $\Delta t$  is the sum of the pulse energies within  $\Delta t$  and within the angle of acceptance equal to  $\alpha_{\text{max}}(\Delta t)$ . Comparing all ratios of AE to AEL (for all possible evaluation durations and start positions) identifies the first pulse as critical for the reduced pulse criterion, i.e. criterion 3). All parameters relevant to this calculation are detailed in Tab. 1 for several evaluation durations (not all applicable choices of the evaluation duration are shown). Application of the other classification rules shows that criterion 3) is the most restrictive one in this example.

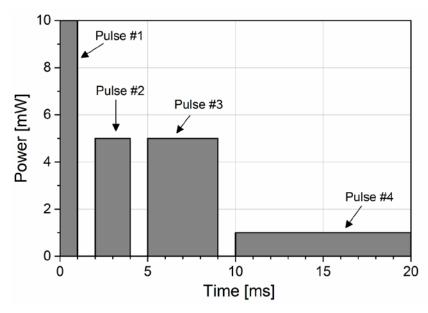


Fig. 1. Arbitrary example of an irregular pulse pattern, consisting of four pulses within  $T_2$ .

Table 1. Application of the reduced pulse criterion to the pulse pattern shown in Fig. 1 for several evaluation durations and according to the proposed definition of N (example for an angular subtense of the image of the apparent source of 10 mrad and a wavelength in the visible wavelength range). For the determination of N, both numerator and denominator were taken as the total energy passing through the 7 mm aperture stop, i.e. determined with an open field of view (FOV) not limited to  $\alpha_{max}$ . The same ratio would result when any other field of view were used, such as  $\alpha_{max}$ .

Parameter	Pulse #1	Pulse #2	Pulse #3	Pulses #1 and #2	Pulses #2 and #3	Pulses #1 to #3
evaluation duration $\Delta t$ [ms]	1	2	4	4	7	9
$\alpha_{\max}(\Delta t)$ [mrad]	6.3	8,9	12.6	12.6	16.7	19.0
$C_6$	6.3 / 1.5 = 4.2	6.0	6.7	6.7	6.7	6.7
$AEL_{single}(\Delta t) [\mu J]$	$7{\times}10^{4}{\cdot}C_6{\cdot}t_1{}^{0.75}\;J=16.6\;\mu J$	39.5	74.2	74.2	112.9	136.4
Energy $Q_{T_2}$ open FOV [ $\mu$ J]	50	50	50	50	50	50
Energy $Q_{\Delta t}$ open FOV [ $\mu J$ ]	10	10	20	20	30	40
N	50 / 10 = 5	5	2.5	2.5	1.67	1.25
$C_5$	$N^{-0.25} = 0.67$	0.67	0.80	0.80	0.88	0.95
$AEL_{s.p.train}(\Delta t)$ [µJ]	11.1	26.4	59.0	59.0	99.4	129.0
$AE(\Delta t)$ [ $\mu J$ ]	$10 \ \mu J \cdot (6.3 \ mrad/10 \ mrad)^2 = 4 \ \mu J$ (see Eq. (6))	8	20	20	30	40
AE / AEL <sub>s.p.train</sub>	0.36	0.30	0.34	0.34	0.30	0.31

For the exact same pulse pattern but with an angular subtense of the image of the apparent source of 40 mrad, the most restrictive result is still found for the reduced pulse criterion, but in this case for the group consisting of the first three pulses, i.e. for an evaluation duration of 9 ms, for which N = 1.25.

These examples demonstrate the application of the parameter N based on relative energy instead of an actual number of pulses, as well as the dependence of the result on other characteristics (especially pulse period and source size) due to the time-dependent parameter  $\alpha_{\text{max}}(\Delta t)$ .

#### B. Validation strategy

In order to test the above definition of N and ensure that all applicable IPTs can be properly assessed under one simple definition, it was decided to adopt an empirical approach. This approach was justified by the number of parameters that characterize an IPT and that have an impact on the injury threshold, namely pulse duration, peak power, duty cycle and number of pulses. A wide variety of possible emission patterns result, that can neither be validated analytically nor by applying general biophysical principles. However, general biophysical principles were used to design the proposed definition of N on the grounds that thermally induced injuries are non-linear both with pulse energy and with pulse duration. The relationship between injury buildup and pulse energy can be modelled by the Arrhenius integral and is illustrated in the following example. Let us consider a pulse pattern that consists of two thermally independent pulses (i.e. sufficient cooling between pulses) of equal duration and the second pulse having half the peak power of the first one. Thus, the second pulse has 33 % of the total energy of the group. The Arrhenius integral with the strong non-linearity of injury with temperature dictates that the second pulse will contribute considerably less than 33 % to the injury buildup, i.e. considerably less than its energy relative to the total pattern energy. Since the factor  $C_5$  is given as  $N^{-0.25}$ , the authors were inclined to believe that the non-linearity of the Arrhenius integral would not be outweighed by the relaxation of  $C_5$  resulting from N being < 2 in this example. Previously published work on IPT with constant pulse duration [7] supports this reasoning. Furthermore, the time-dependence of the AEL (AEL proportional to  $t^{0.75}$ ) similarly favors a definition of N based on relative energy since the timedependence of thermally-induced injuries on pulse duration is shallower than  $t^{0.75}$ . It is, however, not possible to demonstrate conclusively the validity of the proposed method on that basis only.

Consequently, a large number of hypothetical emissions was generated and a computer model that was developed to predict retinal injury thresholds (THR) in the thermal regime was used to compare the THR to the applicable AELs for every single emission. The success of the proposed definition for N was measured by the ratio of THR to AEL and referred to as reduction factor (RF). It is commonly accepted in the laser safety community [9, 10] that the RF shall not be smaller than two, i.e. the accessible emission limit shall be at least a factor of 2 below the injury threshold expressed as ED<sub>50</sub> level in order for laser products classified as Class 1 to be interpreted as safe.

#### C. Database

A computer program was written in order to generate a large database of pulse patterns, organized into five series for a total of 18,000 pulse patterns. The generation was based on a set of parameters that define the pulse pattern (see Tab. 2). The value of a parameter was determined by a random number generated in the unit interval [0,1] and then scaled to the interval set for the respective parameter. An interval can be either continuous or discretized. The distribution of random numbers was governed according to one of the following six weighting functions: uniform (1), linear decrease (2), linear increase (3), exponential decrease (4), exponential increase (5) or parabolic (6). All parameters and the weighting of their respective random number are summarized in Tab. 2. The most relevant parameters are also illustrated in Fig. 2.

Table 2. List of parameters used to generate pulse patterns and range of values for the five series. For each parameter, the type of weighting function of the random number is indicated in parenthesis.

Parameter	Series 1	Series 2	Series 3	Series 4	Series 5
Pulse pattern duration [s]	$10^{-5} - 10$	$10^{-5} - 10$	$10^{-5} - 10$	$10^{-5} - 10$	$10^{-5} - T_2$
Number of subpatterns*	1 - 50(2)	1 - 200(2)	1 – 1000 (2)	1 – 1000 (2)	100 – 1000 (1)
Number of pulses per subpattern	1 – 200 (2)	1 – 200 (2)	1 – 500 (2)	1 – 200 (2)	1 – 200 (2)
Total number of pulses	1 - 1000	1 - 3000	1 - 5000	1 - 5000	1 - 5000
Pulse duration** [s]	$10^{-5} - 0.1(1)$	$10^{-5} - 0.1(1)$	10-4 – 0.1 (1)	10 <sup>-5</sup> – 0.1 (6)	$10^{-5} - 0.1$ (6)
Probability of change for pulse duration [%]	0 – 100 (1)	0 – 100 (1)	0 – 50 (2)	0 – 100 (2)	0 – 100 (2)
Magnitude of change for pulse duration $[\log(t)]$	0 – 4 (2)	0 – 4 (2)	0 – 3 (2)	0 – 4 (6)	0 – 4 (6)
Pulse-to-pulse duty cycle (PPDC) [%]	10 – 95 (3)	10 – 95 (3)	10 – 95 (3)	10 – 95 (3)	10 – 95 (3)
Probability of change in PPDC [%]	0 – 100 (1)	0 – 100 (1)	0 – 100 (1)	0 – 100 (1)	0 – 100 (1)
Peak power envelop	1 - 5(1)	1 - 5(1)	5 (1)	6(1)	6 (1)
Envelop periodicity***	0 - 1(1)	0 - 1(1)	0 - 1(1)	0 - 1(1)	0 - 1(1)
Number of envelop cycles	0.5 – 10 (4)	0.5 – 10 (4)	0.5 – 10 (1)	0.5 – 10 (1)	0.5 – 10 (1)

<sup>\*</sup> a pulse pattern consists of the assembly of numerous subpatterns

The total duration of the pulse pattern as well as the total number of pulses are not input parameters for the pulse pattern generation and are therefore not associated with a random number. If the pulse pattern generated by the computer program exceeds the maximum values set for either pulse pattern duration or total number of pulses, then the pulse pattern is shortened accordingly. For instance in series 1, the pulse pattern cannot last longer than 10 s or contain more than 1,000 pulses.

<sup>\*\*</sup> the pulse duration was discretized with three values per order of magnitude (1, 2 and 4 times 10x)

<sup>\*\*\*</sup> the periodicity of the peak power envelop is either anchored to the subpattern duration (0) or to the duration of 1 s (1)

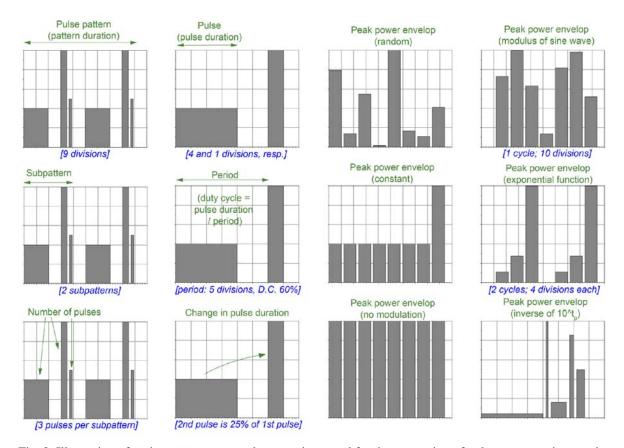


Fig. 2. Illustration of various parameters and conventions used for the generation of pulse patterns; time on the abscissa and power on the ordinate (for each subplot the parameter is indicated at the top and the corresponding numerical value corresponding to the example at hand at the bottom).

Most of the parameters are set at the beginning of the generation process and apply to the whole pattern. However, the two parameters 'probability of change in pulse duration' and 'probability of change in PPDC' were designed to control whether or not the pulse duration or the duty cycle can change between two consecutive pulses. In this case, a random number of value x in the unit interval [0,1] is generated for each pulse of the pattern and compared to the fixed value X of the respective 'Probability of Change' (PoC) parameter. If x < X, then the pulse duration or the duty cycle is allowed to change. This additional procedure allows the generation of pulse patterns with constant pulse duration (e.g. when  $X \to 0$ ) or even regular pulse patterns (when  $X \to 0$  for both PoC parameters and peak power envelop of type 3, 5 or 6). The overall duration of the created pulse patterns also varies: pulse patterns can be of duration  $T_2$ , but they can also be shorter, some only consist of a few pulses. While short pulse trains do not occur very often for the classification of products, they might occur in an MPE analysis, for instance for a laser located on a moving platform.

Finally, the relative peak power of each pulse (peak power envelop in the unit interval [0,1]) can take one of six following forms: random (1), absolute magnitude of a sine function (2), constant (3, in this case, all pulses but the last one have the same peak power; the last pulse of the pattern is set to 1), exponential (4), no modulation (5, all pulses have the same peak power) or inversely proportional to 10 to the power of the pulse duration (6). The maximum peak power within the emission is normalized to 1. The temporal pulse shape was invariably rectangular (constant peak power during the pulse duration). Four pulse patterns generated in this manner are shown in Fig. 3 to illustrate the range of types of pulse patterns obtained by the pseudorandomized generation process.

The number and the variation of pulse patterns is believed to provide a sufficient basis for a general validation of the proposed method.

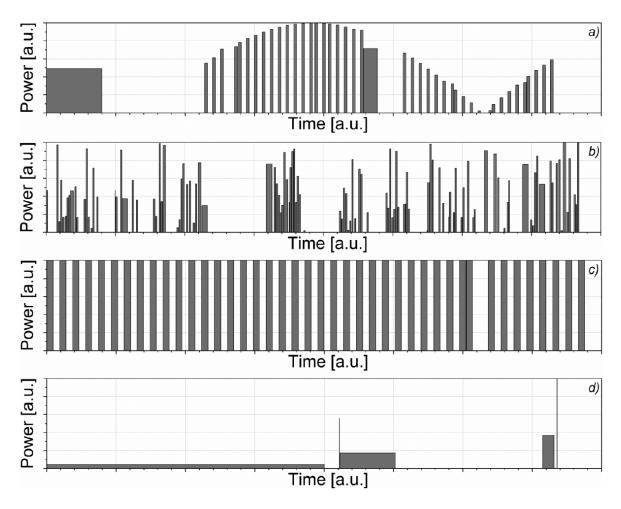


Fig. 3. Four pulse trains chosen arbitrarily in the database for their varied characteristics: #19 exhibits a sine envelop as well as occasionally variable duty cycle and pulse duration (a), #5732 exhibits constantly varying duty cycle and random peak power (b), #6026 is almost regular with constant peak power and constant pulse duration (c) and #13613 contains both short and long pulses (d).

#### D. Retinal injury thresholds

Injury thresholds (THR) of the retina were predicted by a computer model [10] that was validated against in-vivo experiments on non-human primates. The model is based on bulk homogeneous heating of the retina and therefore applies to thermal injury. The finite-element method is used to solve the heat conduction equation in a layered environment representing the retinal tissues and the Arrhenius equation is applied to the temperature history in order to determine the injury threshold level within the RPE layer. Heating of individual melanosomes, which is relevant in the nanosecond and short microsecond regime, cannot be modelled and therefore the injury thresholds related to micro-cavitation (see e.g. [8]) cannot be predicted. Consequently, the validity of the computer model is restricted to pulse durations longer than about  $100 \, \mu s$ . For completeness, pulse durations in the transition range (of  $10 \, \mu s$ ,  $20 \, \mu s$  and  $40 \, \mu s$ ) were included in the calculations. According to this model, the resulting THR is a prediction of the experimental ED<sub>50</sub> level, i.e. the total intraocular energy required to induce a minimum visible lesion

to the retina with a probability of 50 % (see discussion in [11]). In the case of a pulse pattern, the predicted THR is expressed in units of energy and defined for the entire pulse pattern. THR is the intraocular energy level required to reach  $\Omega = 1$  in the Arrhenius integral. In order to obtain THR for the human eye, the following adaptations from the non-human primate model were made:

- 1) the air equivalent focal length of the relaxed human eye was set to 16.68 mm (see Le Grand full theoretical relaxed eye in [12]),
- the retinal image diameter was calculated by multiplying the angular subtense of the image of the apparent source by the focal length of the eye, thus disregarding optical aberrations and scattering of any kind,
- 3) The minimum retinal spot diameter was set to 25 µm and the minimum visible lesion diameter was set equal to 20 µm, in order to account for the fact that such small lesions of the retinal pigmented epithelium might be vision impairing even if undetected by ophthalmoscopic means [13].

It is emphasized that the above adjustments are a set of conservative assumptions. Whenever exposure conditions and endpoints were comparable, injury thresholds for humans were shown to be consistently higher than for non-human primates [14]. The THR was calculated for each of the 18,000 emissions and for six different values of the angular subtense of the image of the apparent source  $\alpha$  in the range between 5 mrad and 100 mrad where the reduction factor  $C_5$  applies. The irradiance distribution of the image of the apparent source was taken to be constant and circular, i.e. a top-hat distribution. All THR were calculated at a wavelength of 530 nm, where the RF for retinal thermal injury is the lowest, as shown in Fig. 4. For  $\alpha = 5$  mrad and  $\alpha = 10$  mrad, the reduction factor can reach values lower than 2.5, with minimum values of 2.1 and 2.3, respectively. The results obtained for wavelengths above 1200 nm are considered irrelevant to this study since the RF is mainly governed by the correction factor  $C_7$  (or  $C_C$  in ANSI Z136.1).

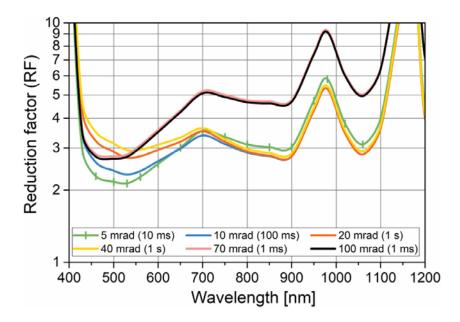


Fig. 4. Ratio of predicted injury threshold, THR, to AEL of Class 1 as a function of wavelength for 5 mrad  $< \alpha \le$  100 mrad for single pulses (for each value of  $\alpha$ , the pulse duration was the one associated with the lowest THR/AEL ratio).

#### E. RF calculation

The figure of merit used to evaluate and validate the tested hypothesis is the ratio of injury threshold (THR) to the accessible emission limit (AEL), referred to as reduction factor (RF). The AEL to be compared with the THR is the one for which the ratio of accessible emission (AE) to AEL is the highest, considering the different criteria to be applied in the case of repetitively pulsed lasers.

Since we are working with theoretical emissions, there is no actual AE. However, the AE/AEL ratios can be calculated with a simulated AE on the basis of the angular subtense of the image of the apparent source  $\alpha$  and for an arbitrary maximum peak power level P within the pulse pattern, as shown in Eq. (6) for M consecutive pulses within  $\Delta t$ . This definition applies to any pulse or groups of pulses and therefore to all classification rules. In the case of the reduced pulse criterion, pulse grouping is limited to a maximum grouping duration of 0.25 s and in the case of the average power criterion to  $T_2$  for Class 1 or 0.25 s for Class 2. In Eq. (6), the power  $P_m$  is defined as the peak power passing through the 7 mm aperture stop (not limited by a field of view), so that  $P_m \cdot t_m$  can be considered as total intraocular energy, the energy per pulse passing through the 7 mm aperture stop. It is necessary to take into account that for the case that the image of the apparent source is larger than  $\alpha_{max}$ , the angle of acceptance for the determination of the AE is limited to  $\alpha_{max}$ , so that the AE is smaller than the total energy that passes through the 7 mm aperture stop. For a top-hat distribution of the retinal image, the reduction factor is equal to the square of the ratio of  $\alpha_{max}$  over  $\alpha$ . A detailed discussion of the correction is given by Schulmeister et al. [15].

$$\begin{cases} AE = \sum_{m=1}^{M} P_m \cdot t_m & \text{for } \alpha \leq \alpha_{max} \\ AE = \left[\frac{\alpha_{max}}{\alpha}\right]^2 \sum_{m=1}^{M} P_m \cdot t_m & \text{for } \alpha > \alpha_{max} \end{cases}$$
 (6)

The first step in the validation for a given pulse pattern is to determine the most restrictive AEL, i.e. the AEL that is associated with the largest ratio of AE to AEL, based on the variation of the evaluation duration  $\Delta t$  (in terms of duration as well as start position) as well as for all multiple pulse criteria. We note that, as given in IEC 60825-1, the AEL( $\Delta t$ ) is determined with a factor  $C_6$  where the value of  $\alpha$  is limited to  $\alpha_{\text{max}}(\Delta t)$  and the AE( $\Delta t$ ) is determined as given by equation (6). In a second step, the most restrictive AEL is compared with the THR. Since the THR is defined for the entire pulse pattern and it is not possible to extract a "sub-THR" for a subset of pulses, it is necessary to scale the AEL to the entire pulse pattern. The scaling takes into account the energy outside the duration  $\Delta t$ , which is the duration for which the AEL( $\Delta t$ ) applies. The scaling factor is equal to the ratio of the energy  $Q_{T_2}$  (the sum of the energies of the pulses within T<sub>2</sub>; the pulse train can also be shorter than  $T_2$ ) and the energy  $Q_{\Delta t}$  within the evaluation duration (that was identified as the critical evaluation duration in the first step). Also, for the case that the retinal image is larger than  $\alpha_{\max}(\Delta t)$ , the scaled AEL( $\Delta t$ ) is increased by the ratio of  $(\alpha/\alpha_{\text{max}}(\Delta t))^2$  as shown in Eq. (7). For an analysis based on IEC 60825-1, the inverse of this factor is applied to reduce the AE (compare Eq. (6)), where the AE( $\Delta t$ ) is defined as the energy passing through the defined field of view, which is limited to  $\alpha_{\max}(\Delta t)$ . The increase-factor applied to the AEL( $\Delta t$ ) considers that the AEL( $\Delta t$ ) is to be compared against the THR, and the THR is defined as total intraocular energy (the energy passing through the pupil of the eye) and not as energy within the angle of acceptance equal to  $\alpha_{\max}(\Delta t)$ . That is, this factor increases the AEL( $\Delta t$ ) to a level that is applicable to the total energy entering the 7 mm aperture stop (see also [15]). A reader familiar with ANSI Z136.1 will note that the AEL increase factor used here follows the same concept as increasing  $C_{\rm E}$  beyond  $\alpha_{\rm max}$ with  $\alpha^2$  and comparing the respective MPE (or AEL) against the total energy passing through the 7 mm aperture. In Eq. (7) the term  $Q_{T_2}$  refers to the energy for the entire pulse pattern, of duration up to  $T_2$ , for which the injury threshold is defined.

$$\begin{cases}
AEL_{7mm\_T2} = AEL \cdot \frac{Q_{T2}}{Q_{\Delta t}} & \text{for } \alpha \leq \alpha_{max} \\
AEL_{7mm\_T2} = AEL \cdot \frac{Q_{T2}}{Q_{\Delta t}} \cdot \left[\frac{\alpha}{\alpha_{max}}\right]^2 & \text{for } \alpha > \alpha_{max}
\end{cases}$$
(7)

The diagram shown in Fig. 5 schematically demonstrates the process of AEL calculation and the comparison with the THR.

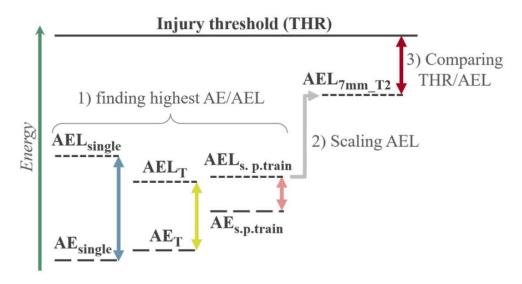


Fig. 5. Illustration of the relationship between accessible emissions (AEs), accessible emission limits (AELs) and injury threshold (THR) in the case of a repetitively pulsed emission. For the validation of the proposed method to determine  $C_5$  for a given pattern, the AEL with the largest ratio of AE/AEL is identified first, then that AEL is scaled to a value that is applicable to the total intraocular energy within the pulse pattern, finally the scaled AEL can be compared against the injury threshold for the pulse pattern that was determined with the computer model.

#### III. RESULTS

The distribution of RF is illustrated in Fig. 6 and reported in Tab. 3 as a function of  $\alpha$  for the 18,000 computer-generated pulse patterns in the range of angular subtenses of the image of the apparent source  $\alpha$  where the correction factor  $C_5$  is applicable. It can be seen that the RF was consistently equal to or larger than 2 with an overall median value of 5.

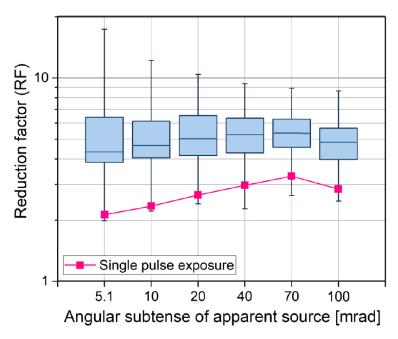


Fig. 6. Distribution of RFs for the database of 18,000 emissions and various values of  $\alpha$ ; the lower and upper bars represent the minimum value and 99<sup>th</sup> percentile, respectively; the box limits represent the 1<sup>st</sup> quartile, median value and 3<sup>rd</sup> quartile (a minimum value of  $\alpha = 5.1$  mrad was used, since  $C_5 = 1$  for  $\alpha \le 5$  mrad).

Table 3. Summary statistics of the RF distribution obtained for irregular pulse trains.

Parameter	5.1 mrad	10 mrad	20 mrad	40 mrad	70 mrad	100 mrad
99 <sup>th</sup> percentile	17.4	12.2	10.4	9.4	8.9	8.6
3 <sup>rd</sup> quartile	6.4	6.1	6.5	6.4	6.3	5.7
Median	4.3	4.7	5.0	5.3	5.4	4.8
1st quartile	3.9	4.0	4.2	4.3	4.6	4
Minimum RF	2.0	2.2	2.4	2.3	2.6	2.5
Min. RF (single pulse*)	2.1	2.3	2.6	2.9	3.3	2.8

<sup>\*</sup> restricted to emission durations between 10 µs to 100 s

For most values of  $\alpha$ , the minimum RF corresponds closely to the lowest RF found for a single pulse. However in some cases, the RF found for an irregular pulse train is somewhat lower than that of a single pulse. This outcome was found for a specific type of pulse pattern containing a few short pulses (typically less than 100  $\mu$ s) combined with a series of longer pulses with relative low peak power. An example is shown in Fig. 7, where the pulses with relative peak power below 5 % of the highest peak power are neglected for the determination of N and the most restrictive AEL was either found for the reduced pulse criterion with a low value for N (typically less than 10) or for the average power criterion, mostly for long pulse patterns and large retinal images (typically above 20 mrad).

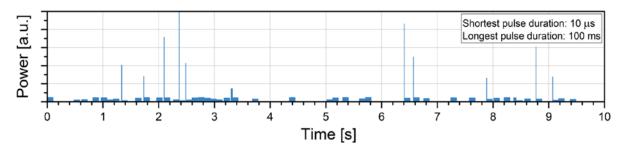


Fig. 7. Illustration of a typical emission (emission # 12783) leading to a lower RF (in this case RF = 2.7) than the lowest RF obtained for a single pulse with  $\alpha = 70$  mrad.

The tendency of the average power criterion to govern long pulse patterns, lasting between approximately 10 s and up to  $T_2$  is evident in Fig. 8a, where it concerns 0.10 % of the 18,000 emissions for  $\alpha = 20$  mrad (and up to 1.4 % for  $\alpha = 100$  mrad).

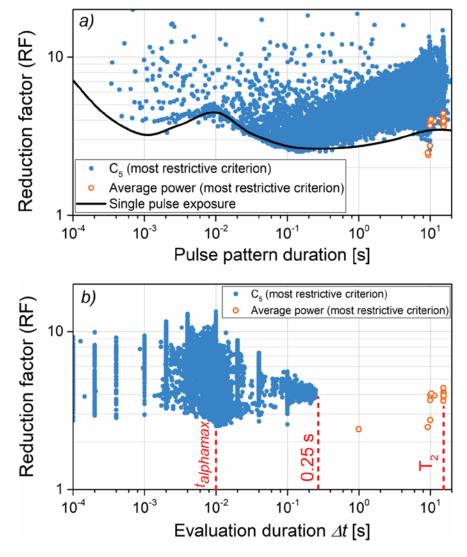


Fig. 8. Distribution of RF for  $\alpha$  = 20 mrad as a function of (a) pulse pattern duration and (b) the evaluation duration found for the most restrictive AE/AEL ratio (open orange circles and blue circles for pulse patterns restricted by the average power or reduced pulse criterion, respectively).

Additionally, it is worth mentioning that the time where  $\alpha = \alpha_{max}$  here referred to as  $t_{alphamax}$  and equal to 10 ms for  $\alpha = 20$  mrad – can be identified in the diagram of Fig. 8b. When the reduced pulse criterion is the most restrictive, the RF was found to be the lowest for a pulse duration or group duration equal to  $t_{alphamax}$ . The grouping of pulses is approximately evenly distributed on both sides of  $t_{alphamax}$ , and ranging from a single pulse (see e.g. point clouds at 100  $\mu$ s or 200  $\mu$ s) to pulse groups up to 0.25 s. The results obtained for other values of  $\alpha$  show similar trends.

In order to quantify the impact of the reduced pulse criterion, the  $4^{th}$  series (randomly chosen, 3000 emissions for each of the six values of  $\alpha$ ) was analyzed only with the single pulse and the average power criterion, i.e. setting  $C_5 = 1$  invariably. As illustrated in Fig. 9, the RF is significantly lower, with a minimum value of 1.3. In the absence of reduced pulse criterion, 12 % of the simulated emissions were associated with a value of RF lower than 2. This can be considered as not sufficiently restrictive.

Finally, the impact of the proposed 5 % relative power limit for calculating *N* was investigated by running the RF analysis with the reduced pulse criterion but without the 5 % limit. For the results obtained for the 4<sup>th</sup> series, when the 5 % limit was not applied, the minimum RF was increased from 2.1 to 2.2 and the median RF from 5.4 to 5.6. The impact of the 5 % limit was mostly restricted to long pulse patterns lasting around 10 s or longer. These results validate the proposal to neglect pulses with peak power less than 5 % of the maximum, again noting that at this point in time, the method is validated for pulse durations in the thermal regime.

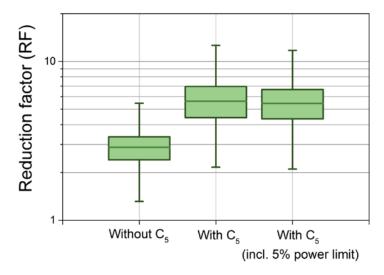


Fig. 9. Distribution of RFs for the 4<sup>th</sup> series of pulse patterns according to various analysis schemes (the lower and upper bars represent the minimum value and 99<sup>th</sup> percentile, respectively; the box limits represent the 1<sup>st</sup> quartile, median value and 3<sup>rd</sup> quartile); see text for more details.

### **IV. CONCLUSIONS**

The safety concerns related to exposure to multiple pulses arose in the 1970s and the first edition of the ANSI standard adopted a correction factor to lower the exposure limit according to the repetition frequency and in later editions according to the number of pulses. Applying the current AELs (or MPEs) and the analysis method in IEC 60825-1 and ANSI Z136.1, it is proposed to revise the definition of N for the determination of the correction factor N for that end, the parameter N is interpreted as a ratio of energy, namely the ratio between the energy within the duration N (or shorter time bases or exposure durations) to the energy within the evaluation duration N used to derive the AEL(Nt) of a single pulse.

For regular pulse patterns this definition (or interpretation) of the parameter N results in the same analysis as for the classic understanding of N, since the ratio of energy within  $T_2$  to the energy of a single pulse is exactly equal to the number of pulses within  $T_2$ . Similarly, for irregular pulse patterns with constant pulse duration and varying peak power, the proposed definition of N is consistent with the interpretation based on relative peak power of ISH1:2017. Furthermore, this interpretation allows both accessible emission and accessible emission limits to be determined for any train of pulses. This applies regardless of the irregularity of the temporal emission, but provided that the pulse pattern does not contain pulses shorter than  $T_i$  since the computer model used to predict retinal injury thresholds can only predict injuries that are thermal in nature. At this point in time, the conclusions of this study cannot be extrapolated to other damage mechanisms, particularly damage due to micro-cavitation in the nanosecond pulse duration regime. The question of whether the proposed interpretation of N can be applied to pulses shorter than the breakpoint  $T_i$  remains to be answered.

In the thermal regime, the results obtained with the proposed analysis method demonstrate that the retinal injury threshold is invariably at least a factor of 2 above the applicable AEL of Class 1. This margin, which is also found for single pulses, is believed to be sufficient in order to qualify emissions that do not exceed the AELs of Class 1 and Class 2 as safe. When the proposed method is applied for classification as Class 3R, we see that predicted injury thresholds may be exceeded, but this also applies to regular pulse trains and is not an effect of the proposed method. The number and variety of possible temporal emissions investigated here allow the conclusion that the proposed interpretation of N is generally applicable in the thermal regime.

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